

# 8-4

# Angles of Elevation and Depression

Warm Up

Lesson Presentation

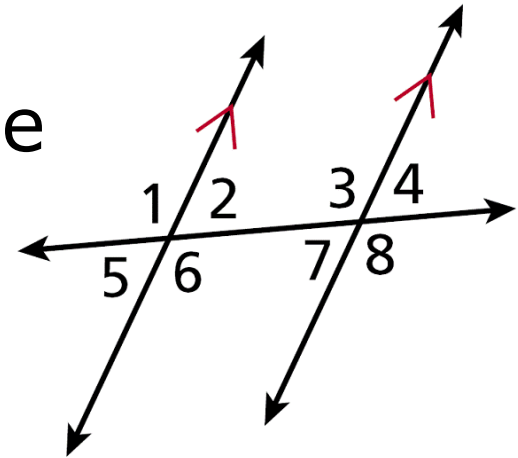
Lesson Quiz

## 8-4 Angles of Elevation and Depression

### Warm Up

1. Identify the pairs of alternate interior angles.

$\angle 2$  and  $\angle 7$ ;  $\angle 3$  and  $\angle 6$



2. Use your calculator to find  $\tan 30^\circ$  to the nearest hundredth. **0.58**
3. Solve  $\tan 54^\circ = \frac{2500}{x}$ . Round to the nearest hundredth.  
**1816.36**

## **8-4** Angles of Elevation and Depression

### ***Objective***

Solve problems involving angles of elevation and angles of depression.

## 8-4 Angles of Elevation and Depression

### ***Vocabulary***

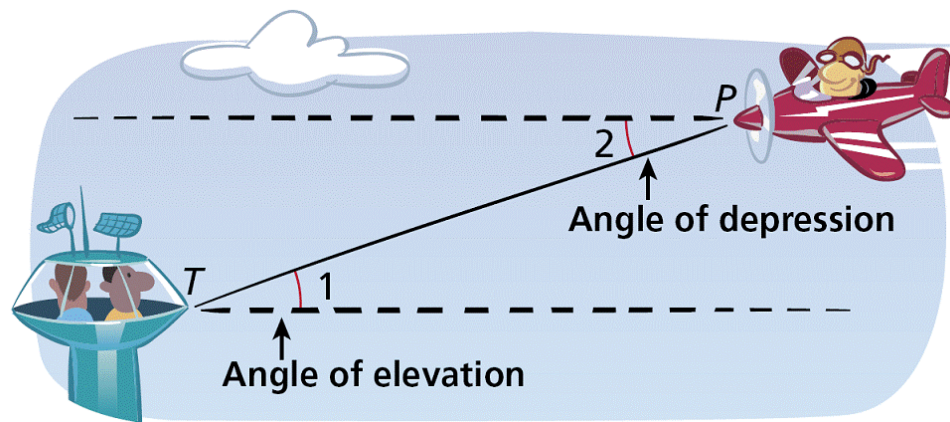
angle of elevation

angle of depression

## 8-4 Angles of Elevation and Depression

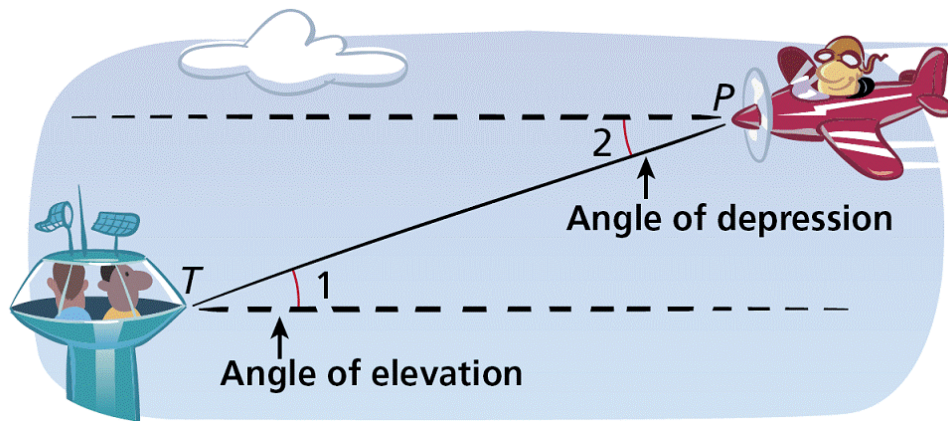
An **angle of elevation** is the angle formed by a horizontal line and a line of sight to a point *above* the line. In the diagram,  $\angle 1$  is the angle of elevation from the tower  $T$  to the plane  $P$ .

An **angle of depression** is the angle formed by a horizontal line and a line of sight to a point *below* the line.  $\angle 2$  is the angle of depression from the plane to the tower.



## 8-4 Angles of Elevation and Depression

Since horizontal lines are parallel,  $\angle 1 \cong \angle 2$  by the Alternate Interior Angles Theorem. Therefore the angle of elevation from one point is congruent to the angle of depression from the other point.

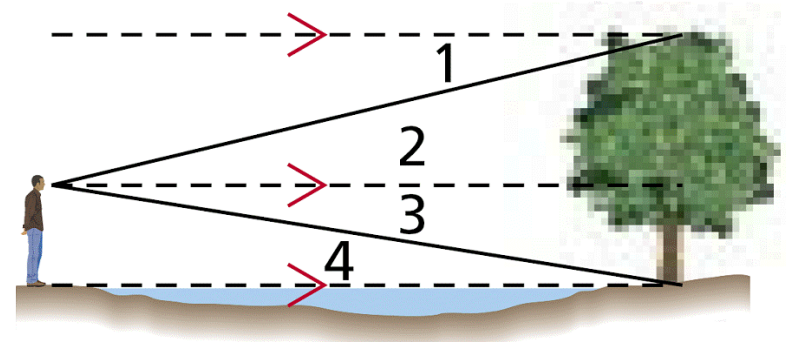


### Example 1A: Classifying Angles of Elevation and Depression

Classify each angle as an angle of elevation or an angle of depression.

$\angle 1$

$\angle 1$  is formed by a horizontal line and a line of sight to a point below the line. It is an angle of depression.



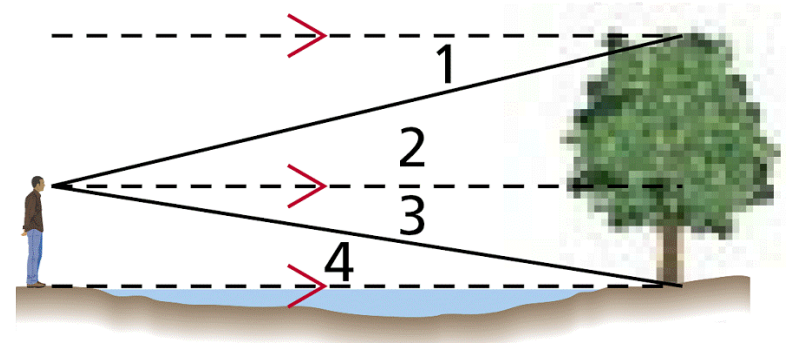


**8-4**

## Example 1B: Classifying Angles of Elevation and Depression

# Classify each angle as an angle of elevation or an angle of depression.

## ∠4



$\angle 4$  is formed by a horizontal line and a line of sight to a point above the line. It is an angle of elevation.



# 8-4 Angles of Elevation and Depression

## Check It Out! Example 1

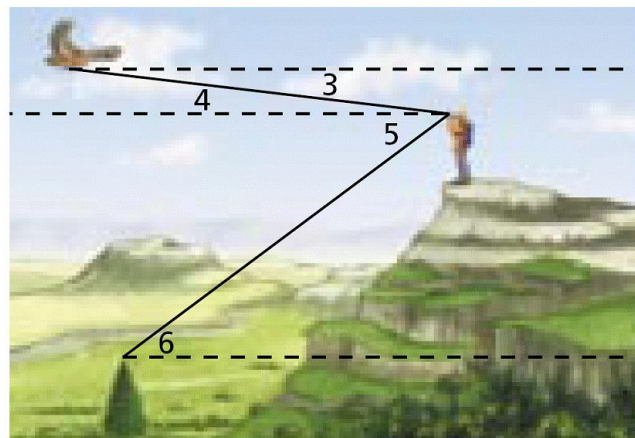
Use the diagram above to classify each angle as an angle of elevation or angle of depression.

1a.  $\angle 5$

$\angle 5$  is formed by a horizontal line and a line of sight to a point below the line. It is an angle of depression.

1b.  $\angle 6$

$\angle 6$  is formed by a horizontal line and a line of sight to a point above the line. It is an angle of elevation.

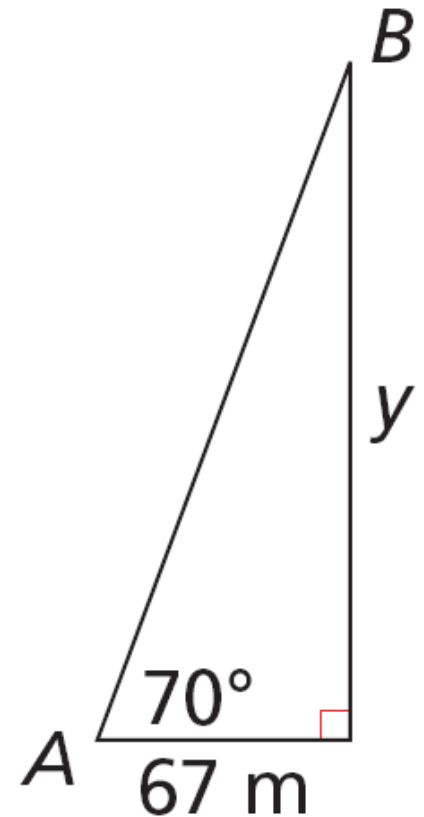


## 8-4 Angles of Elevation and Depression

### Example 2: Finding Distance by Using Angle of Elevation

**The Seattle Space Needle casts a 67-meter shadow. If the angle of elevation from the tip of the shadow to the top of the Space Needle is  $70^\circ$ , how tall is the Space Needle? Round to the nearest meter.**

Draw a sketch to represent the given information. Let  $A$  represent the tip of the shadow, and let  $B$  represent the top of the Space Needle. Let  $y$  be the height of the Space Needle.



# 8-4 Angles of Elevation and Depression

## Example 2 Continued

$$\tan 70^\circ = \frac{y}{67}$$

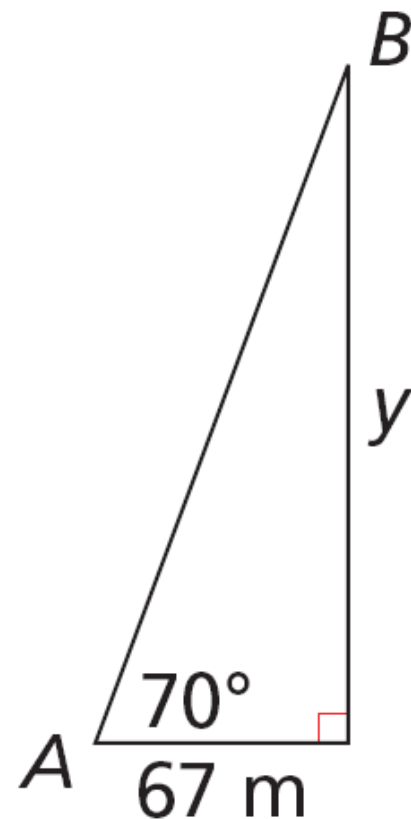
*You are given the side adjacent to  $\angle A$ , and  $y$  is the side opposite  $\angle A$ . So write a tangent ratio.*

$$y = 67 \tan 70^\circ$$

*Multiply both sides by 67.*

$$y \approx 184 \text{ m}$$

*Simplify the expression.*



# 8-4 Angles of Elevation and Depression

## Check It Out! Example 2

**What if...?** Suppose the plane is at an altitude of 3500 ft and the angle of elevation from the airport to the plane is  $29^\circ$ . What is the horizontal distance between the plane and the airport? Round to the nearest foot.

$$\tan 29^\circ = \frac{3500}{x}$$

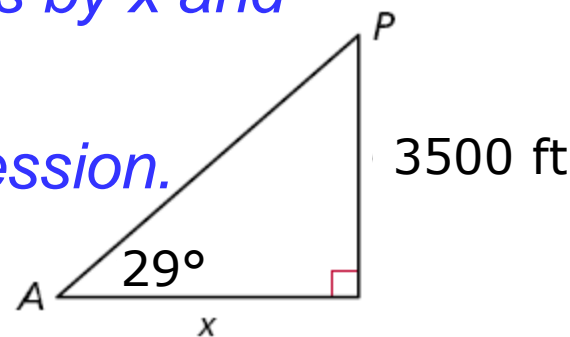
$$x = \frac{3500}{\tan 29^\circ}$$

$$x \approx 6314 \text{ ft}$$

*You are given the side opposite  $\angle A$ , and  $x$  is the side adjacent to  $\angle A$ . So write a tangent ratio.*

*Multiply both sides by  $x$  and divide by  $\tan 29^\circ$ .*

*Simplify the expression.*



## **8-4** Angles of Elevation and Depression

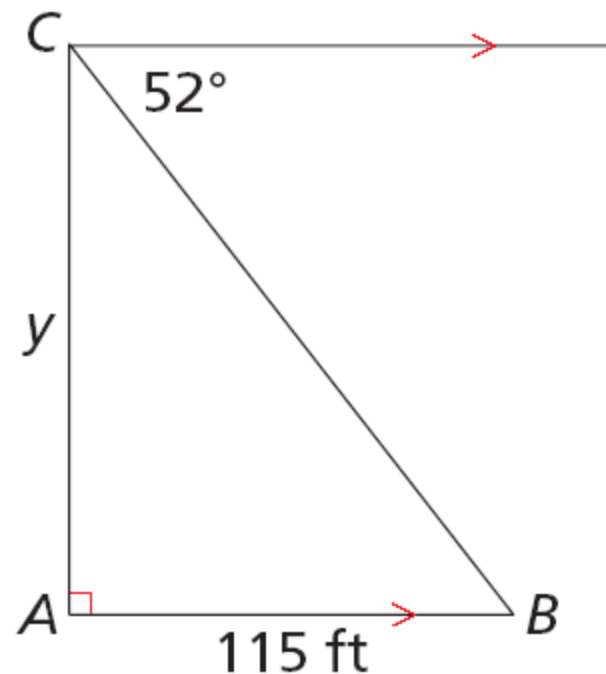
### **Example 3: Finding Distance by Using Angle of Depression**

**An ice climber stands at the edge of a crevasse that is 115 ft wide. The angle of depression from the edge where she stands to the bottom of the opposite side is  $52^\circ$ . How deep is the crevasse at this point? Round to the nearest foot.**

## 8-4 Angles of Elevation and Depression

### Example 3 Continued

Draw a sketch to represent the given information. Let  $C$  represent the ice climber and let  $B$  represent the bottom of the opposite side of the crevasse. Let  $y$  be the depth of the crevasse.



## 8-4 Angles of Elevation and Depression

### Example 3 Continued

By the Alternate Interior Angles Theorem,  $m\angle B = 52^\circ$ .

$$\tan 52^\circ = \frac{y}{115}$$

*Write a tangent ratio.*

$$y = 115 \tan 52^\circ$$

*Multiply both sides by 115.*

$$y \approx 147 \text{ ft}$$

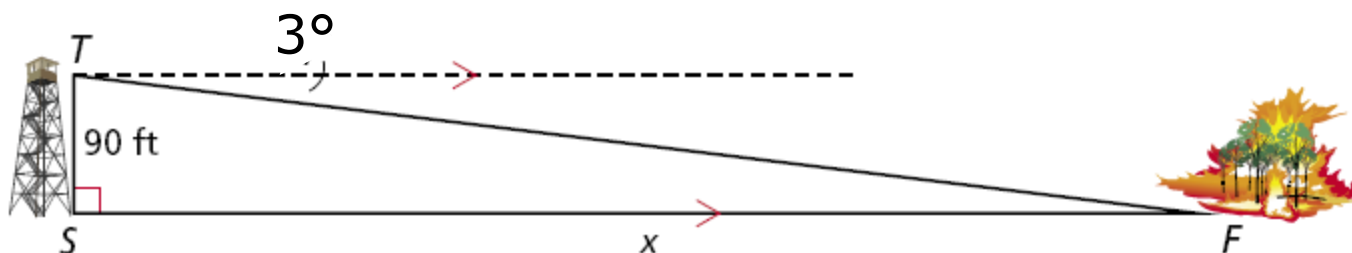
*Simplify the expression.*



## 8-4 Angles of Elevation and Depression

### Check It Out! Example 3

**What if...?** Suppose the ranger sees another fire and the angle of depression to the fire is  $3^\circ$ . What is the horizontal distance to this fire? Round to the nearest foot.



By the Alternate Interior Angles Theorem,  $m\angle F = 3^\circ$ .

$$\tan 3^\circ = \frac{90}{x}$$

*Write a tangent ratio.*

$$x = \frac{90}{\tan 3^\circ}$$

*Multiply both sides by  $x$  and divide by  $\tan 3^\circ$ .*

$$x \approx 1717 \text{ ft}$$

*Simplify the expression.*

## **8-4** Angles of Elevation and Depression

### **Example 4: Shipping Application**

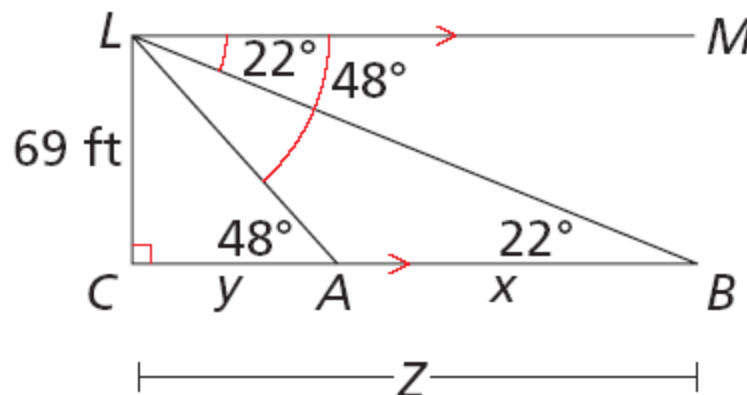
**An observer in a lighthouse is 69 ft above the water. He sights two boats in the water directly in front of him. The angle of depression to the nearest boat is  $48^\circ$ . The angle of depression to the other boat is  $22^\circ$ . What is the distance between the two boats? Round to the nearest foot.**

# 8-4 Angles of Elevation and Depression

## Example 4 Application

**Step 1** Draw a sketch.

Let  $L$  represent the observer in the lighthouse and let  $A$  and  $B$  represent the two boats. Let  $x$  be the distance between the two boats.



## 8-4 Angles of Elevation and Depression

### Example 4 Continued

**Step 2** Find  $y$ .

By the Alternate Interior Angles Theorem,  
 $m\angle CAL = 58^\circ$ .

$$\text{In } \triangle ALC, \tan 48^\circ = \frac{69}{y}.$$

$$\text{So } y = \frac{69}{\tan 48^\circ} \approx 62.1 \text{ ft.}$$

# 8-4 Angles of Elevation and Depression

## Example 4 Continued

**Step 3** Find  $z$ .

By the Alternate Interior Angles Theorem,  
 $m\angle CBL = 22^\circ$ .

$$\text{In } \triangle BLC, \tan 22^\circ = \frac{69}{z}.$$

$$\text{So } z = \frac{69}{\tan 22^\circ} \approx 170.8 \text{ ft.}$$

# 8-4 Angles of Elevation and Depression

## Example 4 Continued

**Step 4** Find  $x$ .

$$x = z - y$$

$$x \approx 170.8 - 62.1 \approx 109 \text{ ft}$$

So the two boats are about 109 ft apart.

## **8-4** Angles of Elevation and Depression

### **Check It Out!** Example 4

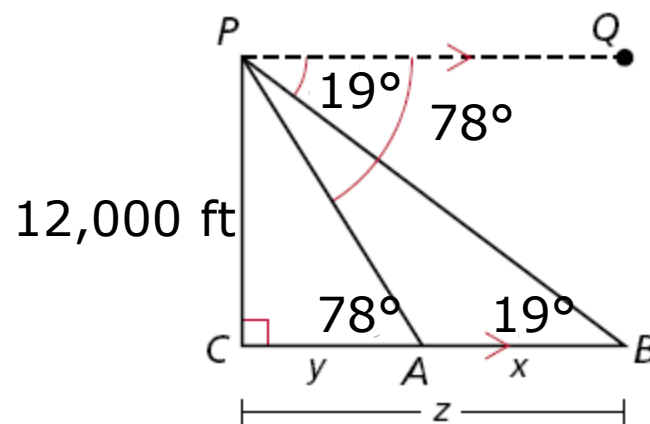
**A pilot flying at an altitude of 12,000 ft sights two airports directly in front of him. The angle of depression to one airport is  $78^\circ$ , and the angle of depression to the second airport is  $19^\circ$ . What is the distance between the two airports? Round to the nearest foot.**



# 8-4 Angles of Elevation and Depression

## Check It Out! Example 4 Continued

**Step 1** Draw a sketch. Let  $P$  represent the pilot and let  $A$  and  $B$  represent the two airports. Let  $x$  be the distance between the two airports.



## 8-4 Angles of Elevation and Depression

### Check It Out! Example 4 Continued

**Step 2** Find  $y$ .

By the Alternate Interior Angles Theorem,  
 $m\angle CAP = 78^\circ$ .

$$\text{In } \triangle APC, \tan 78^\circ = \frac{12,000}{y}.$$

$$\text{So } y = \frac{12,000}{\tan 78^\circ} \approx 2551 \text{ ft.}$$

## 8-4 Angles of Elevation and Depression

### Check It Out! Example 4 Continued

**Step 3** Find  $z$ .

By the Alternate Interior Angles Theorem,  
 $m\angle CBP = 19^\circ$ .

$$\text{In } \triangle BPC, \tan 19^\circ = \frac{12,000}{z}.$$

$$\text{So } z = \frac{12,000}{\tan 19^\circ} \approx 34,851 \text{ ft.}$$

## 8-4 Angles of Elevation and Depression

### Check It Out! Example 4 Continued

**Step 4** Find  $x$ .

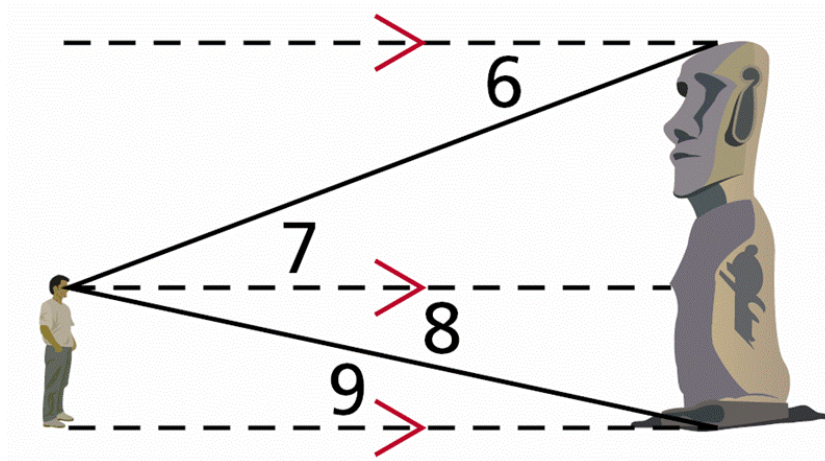
$$x = z - y$$

$$x \approx 34,851 - 2551 \approx 32,300 \text{ ft}$$

So the two airports are about 32,300 ft apart.

## Lesson Quiz: Part I

Classify each angle as an angle of elevation or angle of depression.



1.  $\angle 6$  angle of depression
2.  $\angle 9$  angle of elevation

# 8-4 Angles of Elevation and Depression

## Lesson Quiz: Part II

3. A plane is flying at an altitude of 14,500 ft. The angle of depression from the plane to a control tower is  $15^\circ$ . What is the horizontal distance from the plane to the tower? Round to the nearest foot. **54,115 ft**
4. A woman is standing 12 ft from a sculpture. The angle of elevation from her eye to the top of the sculpture is  $30^\circ$ , and the angle of depression to its base is  $22^\circ$ . How tall is the sculpture to the nearest foot?  
**12 ft**